A Fuzzy Neural CBR Channel Rate Controller for MPEG2 Encoders*

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Abstract- A fuzzy algorithm is used as control surface for the buffer occupancy of a MPEG2 (Moving Picture Experts Group) video encoder. Based on scene features, a supervised algorithm trains a Radial Basis Function Neural Network (RBFNN). The so trained RBFNN acts as a predictor for the number of bits generated in a frame, so that the predicted buffer occupancy can be determined. The predicted and present buffer occupancies are applied to the fuzzy-generated control surface which yields the encoder quantizer step parameter. We compare the obtained results with the Test Model 5 standard rate control scheme.

1. Introduction

The MPEG-2 standard is a widely accepted video-compression technique that applies no standardization to the coding process, allowing the proposal of different approaches for the encoders. The MPEG coded data can be transmitted through constant bit rate (CBR) channels or through variable bit rate (VBR) channels. In the CBR case, due to the highly time-varying complexity of the video sequences, it is imperative the use of a buffer in order to properly stabilize the output rate to the channel [6]. As an example, perhaps one of the most demanding CBR buffer control tasks occurs in the transmission of medical images, where the requirements for image quality are severe and channel rates as low as 2 Mbps are not uncommon [8].

In a previous work [1] the authors developed a non-linear predictive video bit rate controller that uses a supervised RBFNN approach. The RBFNN training is carried out by updating the output neuron synapse weights, as well as the Gaussian centers, by means of the Stochastic Gradient (SG) algorithm [4]. The SG algorithm uses an error input derived from the desired output, which characterizes it as a supervised training process. The rate prediction at the RBFNN output is then applied to a non-linear mapping [2], which yields the encoder quantizer step ($m_{quant}$ parameter [3]).

In this work we present a fuzzy approach to determine the encoder quantizer step. The fuzzy controller implements a family of piecewise lines, each one with a different slope. The line set is conceived to properly control the buffer occupancy for time-varying complexity video signals. The obtained results with such simple rate control technique are similar to those previously obtained by the authors using the referred non-linear mapping technique [1]. In comparison with the Test Model 5 (TM5) standard rate control scheme [3], superior performance was obtained for the buffer occupancy and signal-to-noise ratio (SNR).

2. RBF Neural Networks

A RBF neural network is a universal approximator [4]. It consists of an input layer with $M$ nodes, a hidden layer with $K$ neurons and an output neuron layer. In our case, since we are interested in estimating just the scene complexity on a frame by frame basis, the output layer has only one output neuron, as can be seen in Figure 1 [5].

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The $k^{th}$ hidden neuron, $k=1,\ldots,K$, computes the distance between the center vector $L_k \in \mathbb{R}^M$ and the $n^{th}$ input vector $u(n)\in \mathbb{R}^M$ presented to the RBF. The resulting distance is utilized as argument to a Gaussian function $\varphi$ with variance $\sigma_k^2(n)$ as given by

$$
\varphi(u(n), L_k(n), \sigma_k^2(n)) = \exp\left[ -\frac{1}{\sigma_k^2(n)} \|u(n) - L_k(n)\|^2 \right] \tag{1}
$$

The output of the $k^{th}$ hidden neuron is applied to the output neuron through the weighting synaptic weights $w_k$. The RBF output $y$ to the input vector $u$ is given by the weighted sum of all hidden neurons outputs, according to

$$
y = \sum_{k=1}^{K} w_k \varphi(u(n), L_k, \sigma_k^2(n)) + w_0 \tag{2}
$$

The term $\varphi(u(n), L_k, \sigma_k^2(n))$ in equation (2) is formally defined as the $k^{th}$ Radial Basis Function, which computes the distance $D = \|u - L_k\|$ between the input vector $u$ and the center vector $L_k$ [4]. Notice that the output of each hidden neuron is a non-linear function of $D$. The synaptic weight $w_k$ represents the gain of the path which connects the output of the $k^{th}$ hidden neuron to the output neuron. The constant term $w_0$ is the bias applied to the RBF.

The RBF training is performed by presenting a set of training vectors $u$ to the network input. Upon the presentation of the $n^{th}$ training vector $u(n)$ and the associated desired output $y(n)$, the RBF free parameters $w_k, L_k$ and $\sigma_k^2$ are updated by means of the SG algorithm [4][5], as shown by

$$
w_k(n+1) = w_k(n) + \mu_e(n) \varphi(u(n), \sigma_k^2(n), L_k(n)) \tag{3}
$$

$$
L_k(n+1) = L_k(n) + 2\mu_e(n) w_k(n) \varphi(u(n), \sigma_k^2(n), L_k(n)) \frac{u(n) - L_k(n)}{\sigma_k^2(n)} \tag{4}
$$

And

$$
\sigma_k^2(n+1) = \sigma_k^2(n) + \mu_e(n) w_k(n) \varphi(u(n), \sigma_k^2(n), L_k(n)) \frac{\|u(n) - L_k(n)\|^2}{\sigma_k^2(n)} \tag{5}
$$

where $e(n) = y_d(n) - y(n)$ is the error associated with the $n^{th}$ presented training vector $u(n)$ and $\mu_e, \mu_w, \mu_\sigma$ are the learning rates for the Radial Basis Functions variances, for the center vectors and for the synaptic weights, respectively.

As the training proceeds, the instantaneous error is minimized and the RBF acquires information about the underlying process associated with the training set. Specifically, the so trained RBF acts as a natural interpolator of the underlying process. It is capable to generate an output $y$ with minimum error (in the mean square sense) for a presented vector $u$ which is not a training vector but lies in its neighborhood. In this sense, the RBF is a non-linear predictor [5].

3. The Fuzzy Predictive Video Bit Rate Controller

Figure 2 shows the block diagram of the fuzzy neural predictive video CBR controller [1][2][5]. The $n^{th}$ training vector at the input of the RBF neural network has 9 components: the variances of $F_{n1}$, $F_{n2}$, and $F_{n3}$; the variances of $(F_{n1} - F_{n2})$, $(F_{n2} - F_{n3})$ and $(F_{n3} - F_{n1})$, $T_{n1}$, $T_{n2}$ and $T_{n3}$; where $F_n$ is the $n^{th}$ video frame at the encoder input and $T_n$ is the type of $F_n$ (1 for I-frames, 0 for P-frames and −1 for B-frames [6]).

The RBF output $y(n)$ is a prediction of the number of bits that will be stored in the buffer by the end of the $n^{th}$ frame coding process. The RBF supervised learning via SG algorithm uses the error $e(n)$ obtained from $y(n)$ and from the encoder output bits $cbf(n)$ generated after the $n^{th}$ frame coding.

$$
F_{n+1} - F_{n+1} \text{.}
$$

![Figure 2: Fuzzy neural predictive video bit rate controller](image)

Notice that adding $y(n)$ to $O(n,j)$ – the present buffer occupancy or the occupancy after the $j^{th}$ macroblock of the $n^{th}$ frame is coded – and subtracting the mean bits-per-frame MBF, we obtain $O_b(n)$ – the predicted buffer occupancy. $O_b(n)$ is an estimate of the buffer occupancy after the $j^{th}$ macroblock of the $(n+1)^{th}$ frame is stored in the buffer [6]. MBF is defined as the ratio of the channel rate [Mbits/s] to the frame rate [frames/s].

The quantizer step $Q$ or $mquant$ [3] is the main control parameter for the buffer occupancy. The $mquant$ control is achieved by means of a fuzzy controller. To perform the control task, the controller is provided with the information about the present buffer occupancy $O(n,j)$ and the predicted buffer occupancy $O_b(n)$. Based on this information it decides which quantizer step $(Q(n))$ will be applied to the encoder.

The input fuzzy linguistic variables ($O$ and $O_b$) and the output fuzzy linguistic variable ($Q$) assume linguistic
values in the set \( S = \{ L_0, L_1, \ldots, L_{12} \} \). The set \( S \) is in ascending order, i.e., \( L_0 \) is associated with the lowest linguistic value and \( L_{12} \) is associated with the highest linguistic value. These thirteen linguistic values define the discrete fuzzy partition of the input and output spaces and were experimentally determined, according to the nature of the control problem. Due to the high sensitivity of the human visual system to image details, we had to use a larger number of values to create the discrete linguistic variable spaces than the usual seven or less partitions \([7]\). The differential variances between consecutive frames have been already considered at the RBFNN input. Therefore, the use of fuzzy linguistic variables that might take into account the buffer occupancy velocity is a redundant procedure. Figure 3 shows the membership functions of the fuzzy sets \( O, O_p \) and \( Q \). All the values in the universes of discourse \( O, O_p \) and \( Q \) are normalized to the interval \([0, 1]\).

![Figure 3: Fuzzy sets associated with the present buffer occupancy \( O \), the predicted buffer occupancy \( O_p \), and the quantizer step \( Q \).](image)

A set of fuzzy control rules is derived from a family of \( Q \times O \) lines parameterized by \( O_p \). Each family member is a pair of connected line segments labeled by the \( O_p \) value, as shown in Figure 4. Each segment in a particular member of the line family has its own slope (which was experimentally determined), and an upper and a lower saturation region limit each family member.

Notice that the higher the predicted occupancy \( O_p \), the higher the slope of each \( Q \times O \) line segment. This aims to prevent the buffer overflow for the situation of a large increase in buffer occupancy such as in drastic scene changes. On the other hand, for an almost empty buffer prediction (lower \( O_p \) levels), the \( Q \times O \) line segments present minimum slope, yielding low \( Q \) values for a wide range of all possible \( O \) values, which avoids buffer underflow. The quantizing operation implies that lower levels for \( Q \) results in higher SNR.

The fuzzy control rules derived from Figure 4 are shown in Table 1. Based on Table 1 we can describe the rules in a linguistic form, for instance, “if \( O \) is \( L_6 \) and \( O_p \) is \( L_6 \), then \( Q \) is \( L_6 \).” This specific rule has the meaning: If the present buffer occupancy is at the medium level and the predicted buffer occupancy is at the medium level, then the quantizer step will have the medium level value.

In this work we present the results obtained from this particular set of fuzzy control rules. However, the implementation of the fuzzy controller allows a great number of different fuzzy rule sets. Each set of rules originated from different line families or from any other family of curves is able to generate new control surfaces for specific purposes.

![Figure 4: Family of \( Q \times O \) lines parameterized by \( O_p \).](image)

**Table 1: Fuzzy control rules for \( Q \).**

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4. Experimental Results

In this section we present two examples in order to compare the performance of the RBF fuzzy predictive video CBR controller with that of the Test Model 5 (TM5) heuristic.

In both cases we used standard video sequences, of size 720x480 pixels, a video input frame rate of 30 frames/s and an output channel rate of 3.5Mbits/s. The RBF learning rates were set to: \( \mu_t = 0.15 \), \( \mu_\sigma = 0.5 \) and \( \mu_\nu = 0.1 \). The buffer size adopted was \( 2 \times MBF = 233333 \) bits, as suggested in the TM5 \([3]\).
In the first case we used the standard video sequence Mobile. Figures 5 and 6 show respectively the SNR and the percent buffer occupancy versus the frame index obtained for this sequence.

Notice that the nominal buffer occupancy as well as the buffer occupancy variance attains values substantially smaller for the fuzzy neural controller than for the TM5 controller. For the fuzzy neural controller, the buffer occupancy is kept around 50% along almost all coding process. However, as we can see in Figure 5, the buffer stabilization does not imply in SNR losses.

![Figure 5: SNR [dB] (Mobile sequence).](image1)

![Figure 6: Percent buffer occupancy for Mobile sequence.](image2)

Figures 7 and 8 show respectively the SNR and the percent buffer occupancy versus the frame index for the juxtaposed sequences Mobile & Kiel. This sequence is obtained with the 30 first frames of the Mobile sequence and the last 30 frames of the Kiel sequence appended to it. The other fuzzy parameters, the RBF parameters and the video parameters are all kept the same.

![Figure 7: SNR [dB] (Mobile & Kiel sequence).](image3)

![Figure 8: Percent buffer occupancy for Mobile & Kiel sequence.](image4)

It is important to note that the two sequence composition introduces a drastic scene change [5]. However, in despite of the drastic scene change, the fuzzy neural controller has kept the buffer occupancy in considerable lower levels, if compared with the TM5 control, for the same SNR levels.

5. Conclusions

A fuzzy technique was proposed in this paper to perform the buffer rate control of a predictive video CBR controller for MPEG2 encoders. The fuzzy control was applied to determine the encoder quantizer step parameter, as a function of the present and predicted buffer occupancies.

Concerning the buffer occupancy and the SNR, the results obtained with the proposed technique are similar to those obtained by the authors with the non-linear mapping technique described in [1]. If compared with the Test Model 5 rate control standard technique [3], the results obtained are superior with respect to the nominal buffer occupancy and the buffer variance, for the same SNR.

The fuzzy techniques applied in this work are quite simple and make room for the use of more elaborate techniques, aiming to improve the fuzzy controller performance. For instance, a controller based on adaptive fuzzy sets may be derived from this implementation. This approach improves the controller performance since it can adapt itself to the video signal statistics.

However, the main contribution of this work is to make possible the generation of empirically or experimentally conceived control surfaces, for specific
purposes other than the CBR goal. The fuzzy controller circumvents the need of analytical functions to describe the control surface, since any conceivable surface can be generated by simply changing the set of fuzzy rules.

References


